## kxkxk 3-Factor Between Groups ANOVA with EMMEANS Follow-ups

The data come from one of several studies of food preference among Nebraska turtle species of various ages and husbandry histories within different ecological contexts and day-rhythms. This 3 -way grew out of an interest in whether food preference was moderated by the age of the turtle, and whether this was different for different species. The original study used 6 foods, 7 species and 5 ages ( $\mathrm{N} \approx 1600$ baby turtles). This example uses a subset of those data, 3 foods, 2 species and 2 ages. We learned early in the research that repeated measures designs produced order effects that could not be counter-balanced (leading to a separate line of research on food preference malleability), so a between subjects design was used here.

About the food stimuli used in this study.

- The crickets were immature House Crickets, of 5-7 mm body length. Animals had been pithed before presentation, so that they were able to move their limbs, but could not escape. Proximate crickets have a substantial odor! Four crickets were presented.
- In order to approximate "carrion" 5-7 mm bits of hamburger were "incubated" for 72 hours in a warm, damp, unsterilized environment. It stank! Four bits were presented.
- The lettuce was fresh mature outer leaves of Romaine lettuce, washed with sterilized water and shredded to a standard size approximating the size of mature "duck weed." 30-40 "shreds" were presented.


## Process:

There are a lot of steps to a complete analysis of a 3-way design. Different patterns of significant and non-significant effects will require different subsets of these. Here's a preview...

## Initial Analysis

- Get descriptive means, plots \& F-tests
- Determine what effects are significant
- Consider what lower-order effects we will need to check for descriptive/misleading patterns
- Consider what lower-order effects are likely to be interesting - based on the aggregations involved


## 3-way Interaction

- Select the set of simple effects that most directly addresses the research question or research hypothesis
- Getting the related cell means \& follow-up analyses
- Describe the pattern of the 3-way
- Compute LSDmmd based on full model error term
- Get the related set of simple 2-way interaction F-tests


## 2-way Interactions

- Get the 2-way interaction plot and the corresponding simple 2-way plots
- Get 2-way estimated semi-marginal means \& follow-up analyses to describe each 2-way interaction
- Why are the "Descriptive" and "Estimated" semi-marginal means different \& which are plotted/tested ?
- Use the related depiction of the 3-way to check each 2-way interaction for descriptive/misleading patterns


## Main Effects

- Get the main effect and corresponding simple effect plots
- Get estimated marginal means \& follow-up analyses to describe each main effect
- Why are the "Descriptive" and "Estimated" marginal means different?
- Use the related depiction of the 3-way to check each main effect for descriptive/misleading patterns


## Initial Analysis

## Get descriptive means, plots \& F-tests

UNIANOVA feeds2 BY species age foodoff
/METHOD=SSTYPE(3)
/PRINT=DESCRIPTIVE
/PLOT=PROFILE(foodoff*age*species)
/DESIGN= species age foodoff species*age species*foodoff age*foodoff species*age*foodoff.
$\leftarrow$ DV by IVs order determines left-to-right ordering of IVs in the Descriptive Statistics table
$\leftarrow$ corrects each effect for all other effects
$\leftarrow$ gets descriptive cell, semi-marginal and marginal means
$\leftarrow$ gets plot of cell means ( $x$-axis *separate lines * graphs )
$\leftarrow$ specify the design including the interaction that is automatically calculates from the IVs specified above)

Arrangement of Descriptive Statistics table and the plots reflects, "This 3-way grew out of an interest in whether food preference was moderated by the age of the turtle, and whether this was different for different species."

Notice that both look at type of food, within each age group, for each species.

| Descriptive Statistics |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Dependent Variable: feedwork |  |  |  |  |  |
| species of turtle | age when turtle was tested | type of food offered | Mean | Std. Deviation | N |
| painted | 3 days | live crickets | 9.3333 | 1.21106 | 6 |
|  |  | ground meat | 1.1250 | 1.12599 | 8 |
|  |  | lettuce | 1.2500 | 1.03510 | 8 |
|  |  | Total | 3.4091 | 3.86263 | 22 |
|  | 3 months | live crickets | 12.6250 | 1.84681 | 8 |
|  |  | ground meat | 12.2500 | 1.83225 | 8 |
|  |  | lettuce | 13.2500 | 1.83225 | 8 |
|  |  | Total | 12.7083 | 1.80529 | 24 |
|  | Total | live crickets | 11.2143 | 2.29309 | 14 |
|  |  | ground meat | 6.6875 | 5.92980 | 16 |
|  |  | lettuce | 7.2500 | 6.36134 | 16 |
|  |  | Total | 8.2609 | 5.53949 | 46 |
| snapper | 3 days | live crickets | 14.1429 | 3.23669 | 7 |
|  |  | ground meat | 15.5714 | 1.13389 | 7 |
|  |  | lettuce | 5.3333 | 1.75119 | 6 |
|  |  | Total | 12.0000 | 4.99473 | 20 |
|  | 3 months | live crickets | 14.4000 | 2.07364 | 5 |
|  |  | ground meat | 14.8571 | 2.91139 | 7 |
|  |  | lettuce | 15.7143 | 1.49603 | 7 |
|  |  | Total | 15.0526 | 2.19782 | 19 |
|  | Total | live crickets | 14.2500 | 2.70101 | 12 |
|  |  | ground meat | 15.2143 | 2.15473 | 14 |
|  |  | lettuce | 10.9231 | 5.60449 | 13 |
|  |  | Total | 13.4872 | 4.14139 | 39 |
| Total | 3 days | live crickets | 11.9231 | 3.47519 | 13 |
|  |  | ground meat | 7.8667 | 7.53910 | 15 |
|  |  | lettuce | 3.0000 | 2.48069 | 14 |
|  |  | Total | 7.5000 | 6.16936 | 42 |
|  | 3 months | live crickets | 13.3077 | 2.05688 | 13 |
|  |  | ground meat | 13.4667 | 2.66905 | 15 |
|  |  | lettuce | 14.4000 | 2.06328 | 15 |
|  |  | Total | 13.7442 | 2.28966 | 43 |
|  | Total | live crickets | 12.6154 | 2.88551 | 26 |
|  |  | ground meat | 10.6667 | 6.24408 | 30 |
|  |  | lettuce | 8.8966 | 6.21257 | 29 |
|  |  | Total | 10.6588 | 5.57322 | 85 |

The "Descriptive Statistics" are the raw or "uncorrected" means.

The marginal means for the main effects are weighted by the differential sizes of the cell means being aggregated.

For example, the marginal mean for painted turtles is

$$
\begin{aligned}
& ((9.333 * 6)+(1.125 * 8)+(1.250 * 8)+ \\
& (12.625 * 8)+(12.250 * 8)+(13.250 * 8)) / 46 \\
& =8.2609
\end{aligned}
$$

Likewise, the semi-marginal means for the 2-way interactions are weighted by the differential sizes of the cell means being aggregated.

For example, the semi-marginal mean for 3day old painted turtles is

$$
((9.333 * 6)+(1.125 * 8)+(1.250 * 8)) / 22
$$



From the means and plots, it looks like younger turtles make more feeding attempts and show little food preference. Older turtles show a food preference, but the preference is somewhat different for Paints \& Snappers.

## Determine what effects are significant

## Tests of Between-Subjects Effects

Dependent Variable: feedwork

| Source | Type III Sum of Squares | df | Mean Square | F | Sig. |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Corrected Model | $2347.132^{\text {a }}$ | 11 | 213.376 | 59.458 | . 000 |
| Intercept | 9747.955 | 1 | 9747.955 | 2716.305 | . 000 |
| species | 526.765 | 1 | 526.765 | 146.785 | . 000 |
| age | 763.475 | 1 | 763.475 | 212.745 | . 000 |
| foodoff | 189.142 | 2 | 94.571 | 26.353 | . 000 |
| species * age | 157.255 | 1 | 157.255 | 43.820 | . 000 |
| species * foodoff | 132.061 | 2 | 66.030 | 18.400 | . 000 |
| age * foodoff | 308.892 | 2 | 154.446 | 43.037 | . 000 |
| species * age * foodoff | 111.318 | 2 | 55.659 | 15.510 | . 000 |
| Error | 261.974 | 73 | 3.589 |  |  |
| Total | 12266.000 | 85 |  |  |  |
| Corrected Total | 2609.106 | 84 |  |  |  |

All 7 effects are significant.
One thing to notice about these data is how small are the standard deviations!

Baby turtles are an amazingly homogeneous group!

So, small mean differences are reliably different \& we get lots of significant effects!!
a. R Squared $=.900($ Adjusted R Squared $=.884)$

## Consider what lower-order effects we will need to check for descriptive/misleading patterns

Because of the significant 3-way, the means patterns of all 6 lower-order effects -- all 3 2-way interactions and all 3 main effects -- will have to be carefully checked against the corresponding higher-order effects to determine if they are descriptive or misleading. Remember, this will have to be done whether the lower-order effect is significant or not - 2 -way and main effect nulls can be misleading!

## Consider what lower-order effects are likely to be interesting - based on the aggregations involved

## Species

- Paints and Snappers represent just 2 of the 7 native Nebraskan species and of the 256 species worldwide. So aggregating across them doesn't represent any important population.
- These two species do represent about $85 \%$ of "pet" turtles sold in the US - but most pets aren't fed these foods at these ages, so the lack of external population \& stimulus validity makes the aggregate of these conditions uninteresting.
- So, the main effect of age (aggregating across species \& foods), the main effect of food (aggregating across species and age) and the age*food interaction (aggregating across species) would only be interesting as a simplifying description if the means pattern was descriptive because it matched the corresponding simple effect means patterns!


## Age

- There are very few behaviors that are age-related such that aggregating 3-day-old and 3-month-old juveniles tells us about an interesting population.
- So, the main effect of species (aggregating across age \& foods), the main effect of food group (aggregating across age and species) and the species*food interaction (aggregating across age) would only be interesting as a simplifying description if the means pattern was descriptive because it matched the corresponding simple effect means patterns!


## Food Offered

- These three foods were very carefully chosen to represent the three major types of foods available to juvenile turtles: 1) available insects, 2) carrion, \& 3) vegetation (specifically duckweed). Therefore, aggregating across these three foods into an "available foods group" would be interesting.
- Still the the main effect of species (aggregating across age \& foods), the main effect of age (aggregating across species and foods) and the species*age interaction (aggregating across foods) would only be interesting as a meaningful aggregation if the means pattern was descriptive because it matched the corresponding simple effect means patterns!

Remember - though we have no such cases to address here - non-significant lower-order effects that are involved in a significant higher order effect must be cwhether they are descriptive or misleading!!!

## 3-way Interaction

## Select the set of simple effects that most directly addresses the research question or research hypothesis

The statement that, "This 3-way grew out of an interest in whether food preference was moderated by the age of the turtle, and whether this was different for different species" makes the selection of the simple effects to use to describe the interaction straightforward.

From this, we'll want to focus on the simple effects of Food Offered within the simple 2-way Food Offered * Age, and then examine how this 2 -way is different for different Species.

## Get the related cell means \& follow-up analyses

/EMMEANS=TABLES ( species * age * foodoff ) compare (foodoff)
$\leftarrow$ "compare (foodoff)" asks for pairwise comparisons among the 3 food off conditions - live crickets, ground meat \& lettuce
$\leftarrow$ "species*age*food" specifies that those pairwise comparisons are made within each age group, for each species

## Estimates

Dependent Variable: feeds

| species of turtle | age when turtle was tested | type of food offered | Mean | Std. Error |
| :--- | :--- | :--- | ---: | ---: |
| painted | 3 days | live crickets | 9.333 | .773 |
|  |  | ground meat | 1.125 | .670 |
|  |  | lettuce | 1.250 | .670 |
|  | 3 months | live crickets | 12.625 | .670 |
|  | ground meat | 12.250 | .670 |  |
|  |  | lettuce | 13.250 | .670 |
| snapper | live crickets | 14.143 | .716 |  |
|  | 3days | ground meat | 15.571 | .716 |
|  |  | lettuce | .773 |  |
|  |  | live crickets | 14.400 | .847 |
|  | 3 months | ground meat | 14.857 | .716 |
|  |  | lettuce | .75 .714 | .716 |

These cell means "Estimates" are the same as the cell mean "Descriptive Statistics" given above and the same means that are plotted above.

The F-tests shown below test the simple effect of Food Offered for every combination of Age \& Species.

For both species, there are Food Offered effects for younger, but not for older, animals.

Univariate Tests
Notice that the MSe for these F-tests is the same as for the full model - based on the full sample size. It is also possible to get these tests by splitting the file into these 4 groups and getting the Foodoff ANOVA for each. However, that approach will use a separately composed error term for each $F$, will have lower power, greater chance of inconsistent effects \& of Type II Errors.

| species of turtle | age when turtle was tested |  | Sum of Squares | df | Mean Square | F | Sig. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| painted | 3 days | Contrast | 289.610 | 2 | 144.805 | 40.350 | . 000 |
|  |  | Error | 261.974 | 73 | 3.589 |  |  |
|  | 3 months | Contrast | 4.083 | 2 | 2.042 | . 569 | . 569 |
|  |  | Error | 261.974 | 73 | 3.589 |  |  |
| snapper | 3 days | Contrast | 388.095 | 2 | 194.048 | 54.072 | . 000 |
|  |  | Error | 261.974 | 73 | 3.589 |  |  |
|  | 3 months | Contrast | 5.462 | 2 | 2.731 | . 761 | . 471 |
|  |  | Error | 261.974 | 73 | 3.589 |  |  |

Each F tests the simple effects of type of food offered within each level combination of the other effects shown. These tests are based on the linearly independent pairwise comparisons among the estimated marginal means.

| species of turtle | age when turtle was tested | (I) type of food offered | (J) type of food offered | Mean Difference (IJ) | Std. Error | Sig. ${ }^{\text {b }}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| painted | 3 days | live crickets | ground meat | $8.20{ }^{*}$ | 1.023 | . 000 |
|  |  |  | lettuce | $8.083{ }^{*}$ | 1.023 | . 000 |
|  |  | ground meat | live crickets | -8.208* | 1.023 | . 000 |
|  |  |  | lettuce | -. 125 | . 947 | . 895 |
|  |  | lettuce | live crickets | -8.083* | 1.023 | . 000 |
|  |  |  | ground meat | . 125 | . 947 | . 895 |
|  | 3 months | live crickets | ground meat | . 375 | . 947 | . 693 |
|  |  |  | lettuce | -. 625 | . 947 | . 511 |
|  |  | ground meat | live crickets | -. 375 | . 947 | . 693 |
|  |  |  | lettuce | -1.000 | . 947 | . 295 |
|  |  | lettuce | live crickets | . 625 | . 947 | . 511 |
|  |  |  | ground meat | 1.000 | . 947 | . 295 |
| snapper | 3 days | live crickets | ground meat | -1.429 | 1.013 | . 163 |
|  |  |  | lettuce | $8.810^{*}$ | 1.054 | . 000 |
|  |  | ground meat | live crickets | 1.429 | 1.013 | . 163 |
|  |  |  | lettuce | $10.238^{*}$ | 1.054 | . 000 |
|  |  | lettuce | live crickets | -8.810* | 1.054 | . 000 |
|  |  |  | ground meat | $-10.238^{*}$ | 1.054 | . 000 |
|  | 3 months | live crickets | ground meat | -. 457 | 1.109 | . 681 |
|  |  |  | lettuce | -1.314 | 1.109 | . 240 |
|  |  | ground meat | live crickets | . 457 | 1.109 | . 681 |
|  |  |  | lettuce | -. 857 | 1.013 | . 400 |
|  |  | lettuce | live crickets | 1.314 | 1.109 | . 240 |
|  |  |  | ground meat | . 857 | 1.013 | .400 |

Based on estimated marginal means
*. The mean difference is significant at the .050 level.
b. Adjustment for multiple comparisons: Least Significant Difference (equivalent to no adjustments).

From the cell means given above and these pairwise results we can explicate the pattern of the 3 -way as...

Crickets v Ground Meat

| Painted Turtles | 3-days <br>  <br> 3 3-months |
| :--- | :--- |

Snapping Turtles 3-days
3-months
$>$
$=$
$=$
$=$
=

Crickets v Lettuce

$$
\begin{aligned}
& > \\
& =
\end{aligned}
$$

$$
=
$$

$$
>
$$

$$
=
$$

Ground Meat v Lettuce
$=$
$=$
$>$
=

## Describe the pattern of the 3-way

In words - following the SE of food for within each age group, for each species ...
For painted turtles, 3-day-olds preferred crickets to ground meat and lettuce, whereas 3-month-olds showed no preference. However, for snappers, the 3-days preferred crickets and ground meat to lettuce, whereas the 3-month-olds showed no preference.

Or, alternatively...
The 3-day-old painted turtles preferred crickets to ground meat or lettuce, while he 3-day old snappers preferred crickets and ground meat to lettuce. The 3-month-old turtles of neither species showed a preference.

For either description, notice that the pattern of the pairwise comparisons guarantees that the main effect of Food Offered and the 2-way interaction of Food Offered * Age will be misleading! In each case, different subsets of data show different means patterns, and, so, they cannot all match the means pattern of the corresponding main effect or 2-way.

## Compute LSDmmd based on full model error term

This is a BG model, so all the F-tests and follow-up analyses are based on a single error term ( $\mathrm{MSe}=111.852$ ), though the Standard Errors of the follow-ups calculated by SPSS vary with sample size. Why care? Because, the follow-up analyses are based on a t-test (that isn't shown in the output) that uses the standard error in the denominator.

So, depending on whether the cells being compared have larger or smaller sample sizes, the standard error can be larger (smaller ns) or smaller (larger ns), and the same cell mean difference can be significant for one comparison and not significant for another!!

An alternative is to use this "full model error term" as the basis for computing an LSDmmd value that is then used to compare any two cell means. This is an extension of the "homogeneity of variance" assumption that is made when we compute the ANOVA error term for BG models. That assumption is that it makes sense to combine the within-group variability from the different design cells, because they each represent a sample taken from different populations that all have the same variability, so the aggregate of them all is the best estimate of the variability of each. The extension in the "full model error term" approach is that since the best estimate is derived from using the full design sample, the significance test should be based on the df from all the participants.

Why do people who like this approach like it?

1. It is based on the same estimate of variability, but larger sample size, and, so, uses a smaller standard error than the pairwise error term approach. So, it provides a more powerful significance test, and more pairwise cell mean comparisons are significantly different using this approach (though the reverse can happen on occasion).
2. This approach provides an easy method for the comparison of nonadjacent cells means. We might want to know whether the mean number of strikes made by 3 -month-old painted turtles offered lettuce (mean $=13.250$ ) is different than by 3 -day-old snappers offered ground meat (mean $=14.857$ ) there is no easy to get SPSS to provide this significance test, but the Computators will give us an LSDmmd that we can use to compare these means. For this analysis $\mathrm{k}=12$ conditions of the $2 \times 2 \times 3$ design, $\mathrm{n}=\mathrm{N} / \mathrm{k}=85 / 12=7 / 083$ \& $\mathrm{MSe}=3.589$. Using the LSDmmd value, we would conclude these two groups have equivalent performances.

| E. LSD/HSD | $\square$ | 回 |
| :---: | :---: | :---: |
| Minimum Mean Difference Computator |  |  |
|  |  |  |
| Number of conditions in the effect |  | 0 |
| n (average number of data points upon which each mean is based) |  | 7.083 |
| Mean Square Error (MSe) |  | 3.589 |
| error degrees of freedom |  | 73 |
| Compute LSD \& HSD minimum mean differences |  |  |
| LSDmmd | 2.025 |  |
| HSDmmd | 0 |  |



## Getting the related set of simple 2-way interaction F-tests

Having decides to describe the 3-way interaction as "the different 2-way interaction pattern of Food Offered and Age for each Species" we might want to have those two simple 2-way F-tests.

SORT CASES BY species.
SPLIT FILE LAYERED BY species.

UNIANOVA feeds BY age foodoff.
$\leftarrow$ sorts the data file into snappers and painted turtles
$\leftarrow$ tells SPSS to compute the requested analyses separately for each split file.
$\leftarrow$ requests the age \& food 2-way ANOVA

Tests of Between-Subjects Effects
Dependent Variable: feeds

| species of turtle | Source | Type III Sum <br> of Squares | df | Mean Square | F | Sig. |
| :--- | :--- | ---: | ---: | ---: | ---: | ---: |
| painted | Corrected Model | $1286.286^{\mathrm{a}}$ | 5 | 257.257 | 108.796 | .000 |
|  | Intercept | 3136.877 | 1 | 3136.877 | 1326.609 | .000 |
|  | age | 881.482 | 1 | 881.482 | 372.786 | .000 |
|  | foodoff | 156.932 | 2 | 78.466 | 33.184 | .000 |
|  | age * foodoff | 165.707 | 2 | 82.854 | 35.039 | .000 |
|  | Error | 94.583 | 40 | 2.365 |  |  |
|  | Total | 4520.000 | 46 |  |  |  |
|  | Corrected Total | 1380.870 | 45 |  |  |  |
|  | Corrected Model | $484.353^{\text {b }}$ | 5 | 96.871 | 19.097 | .000 |
|  | Intercept | 6825.584 | 1 | 6825.584 | 1345.622 | .000 |
|  | age | 104.981 | 1 | 104.981 | 20.696 | .000 |
|  | 161.782 | 2 | 80.891 | 15.947 | .000 |  |
|  | foodoff | 245.396 | 2 | 122.698 | 24.189 | .000 |
|  | age * foodoff | 167.390 | 33 | 5.072 |  |  |
|  | Error | 7746.000 | 39 |  |  |  |
|  | Total | 651.744 | 38 |  |  |  |
|  | Corrected Total |  |  |  |  |  |

a. R Squared $=.932$ (Adjusted R Squared $=.923$ )
b. $R$ Squared $=.743$ (Adjusted R Squared $=.704$ )

Of the various F-tests presented, only the 2-way interactions are interesting/meaningful. These 2-ways analyses each use an error term based on the data and sample size from a single species. As a result, each of these 2 -way F-tests has less power than the 3-way F-test they are being used to explore. So, it is possible to have one of those "significant effects that aren't anywhere"

We can also re-compute these simple 2-way F-tests using the MSage*toodoff from the table above, and the MSerror from the 3way full model ( $\mathrm{MSe}=3.589$ ). This would lead to...

Food Offered * Age for Painted Turtles
82.854
$\mathrm{F}(2,73)=-\underset{3.589}{=-------23.086 \mathrm{p}<.0001}$

Food Offered * Age for Snappers
122.698
$F(2,73)=---------=34.187 \mathrm{p}<.0001$
3.589

## 2-way Interactions

Using the Age*Species 2-way as an example, here is how to get the plot \& follow-ups for that 2-way and the corresponding simple-2-way of Age*Species for each Food Offered.

Get the 2-way interaction plot and the corresponding simple 2-way plots

> /PLOT=PROFILE( species * age )
/PLOT=PROFILE(species * age * foodoff)

## 2-way plot of Species * Age



Simple 2-way plot of Species * Age for Ground Meat
$\leftarrow$ gets plot of estimated semi-marginal means for Species * Age 2-way interaction ( $x$-axis *separate lines)
$\leftarrow$ gets plot of the cell means arranged to check if the pattern of the Species * Age interaction is the same for each Food Offered ( $x$-axis * separate lines * separate graphs)

Simple 2-way plot of Species * Age for Live Crickets


Simple 2-way plot of Species * Age for Lettuce


None of the simple 2-ways looks quite like the 2-way, but it all hinges on the age effects for Snappers. Significance tests can be comforting, concentrating on the simple effects of Age for each Species (for each Food Offered).

Get 2-way estimated semi-marginal means \& follow-up analyses to describe the 2-way interactions
$\leftarrow$ gets pairwise comparisons of estimated age group semi-marginal means for each species - used to describe the pattern of the Species * Age 2-way

## Why are the "Descriptive" and "Estimated" semi-marginal means different \& which are plotted/tested ?

You should notice the estimated semi-marginal means shown in the graphs above and the "Estimates" table below are not the same as the raw semi-marginal means from the "Descriptive Statistics" up above. Those raw semi-marginal means were 3.41 for 3-day Painted, 12.71 for 3-month Painted, 12.00 for 3-day Snappers \& 15.05 for 3-month Snappers.

The difference between the raw and estimated semi-marginal means reflects that the effects in the design are not orthogonal (because of unequal-n). The estimated semi-marginal means are predicted based on the model (not the raw data) and provide for the comparisons among these groups, after correcting for the other effects in the model.


The F-tests compare the corrected/estimated semimarginal means.

The pairwise comparisons are redundant with the F-tests because these are all 2 -group comparisons.

Be sure to check the direction of each significant comparison !!!

Pairwise Comparisons
Dependent Variable: feeds

| species of turtle | (l) age when turtle was tested | (J) age when turtle was tested | Mean Difference (lJ) | Std. Error | Sig. ${ }^{\text {b }}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| painted | 3 days | 3 months | $-8.80{ }^{\text {n }}$ | . 562 | . 000 |
|  | 3 months | 3 days | $8.80{ }^{*}$ | . 562 | . 000 |
| snapper | 3 days | 3 months | $-3.308^{*}$ | . 612 | . 000 |
|  | 3 months | 3 days | $3.308^{*}$ | . 612 | . 000 |

Based on estimated marginal means
*. The mean difference is significant at the .050 level.
b. Adjustment for multiple comparisons: Least Significant Difference (equivalent to no adjustments).

The pattern of the 2-way interaction is...
Painted 3 day $\lll 3$ month
Snapper 3 3-day $<3$ month

The Age effect is the same direction for both Species, but is much larger for Painted turtles.
$\leftarrow$ gets pairwise comparisons of age group cell means at each combination of species and food offered, to check whether the pattern of the species*age 2-way is descriptive or misleading

Estimates

| type of food offered | species of turtle | age when turtle was tested | Mean | Std. Error |
| :---: | :---: | :---: | :---: | :---: |
| live crickets | painted | 3 days | 9.333 | . 773 |
|  |  | 3 months | 12.625 | . 670 |
|  | snapper | 3 days | 14.143 | . 716 |
|  |  | 3 months | 14.400 | . 847 |
| ground meat | painted | 3 days | 1.125 | . 670 |
|  |  | 3 months | 12.250 | . 670 |
|  | snapper | 3 days | 15.571 | . 716 |
|  |  | 3 months | 14.857 | . 716 |
| lettuce | painted | 3 days | 1.250 | . 670 |
|  |  | 3 months | 13.250 | . 670 |
|  | snapper | 3 days | 5.333 | . 773 |
|  |  | 3 months | 15.714 | . 716 |


| Univariate Tests |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Dependent Variable: feeds |  |  |  |  |  |  |  |
| type of food offered | species of | turtle | Sum of Squares | df | Mean Square | F | Sig. |
| live crickets | painted | Contrast | 37.149 | 1 | 37.149 | 10.352 | . 002 |
|  |  | Error | 261.974 | 73 | 3.589 |  |  |
|  | snapper | Contrast | . 193 | 1 | . 193 | . 054 | . 817 |
|  |  | Error | 261.974 | 73 | 3.589 |  |  |
| ground meat | painted | Contrast | 495.063 | 1 | 495.063 | 137.951 | . 000 |
|  |  | Error | 261.974 | 73 | 3.589 |  |  |
|  | snapper | Contrast | 1.786 | 1 | 1.786 | .498 | .483 |
|  |  | Error | 261.974 | 73 | 3.589 |  |  |
| lettuce | painted | Contrast | 576.000 | 1 | 576.000 | 160.505 | . 000 |
|  |  | Error | 261.974 | 73 | 3.589 |  |  |
|  | snapper | Contrast | 348.161 | 1 | 348.161 | 97.016 | . 000 |
|  |  | Error | 261.974 | 73 | 3.589 |  |  |

(from above) The pattern of the 2-way interaction was...
Painted 3 day $\lll 3$ month
Snapper 3-day < 3 month

For live crickets, the corresponding simple 2-way is...

| Painted | 3 day $<3$ month |
| :--- | ---: |
| Snapper | 3-day |

For ground meat, the corresponding simple 2-way is...

| Painted | 3 day | $\lll 3$ month |
| :--- | :--- | :--- | :--- |
| Snapper | 3 -day | $=3$ month |

For lettuce, the corresponding simple 2-way is...

| Painted | 3 day | $\lll<$ | 3 month |
| :--- | :--- | :--- | :--- |
| Snapper | 3 -day | $\lll<3$ month |  |

So, the 2-way interaction pattern is descriptive only for crickets, and is misleading for ground mean \& lettuce.

| type of food offered | species of turtle | (l) age when turtle was tested | (J) age when turtle was tested | Mean Difference (l- $\mathrm{J})$ | Std. Error | Sig. ${ }^{\text {b }}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| live crickets | painted | 3 days | 3 months | $-3.292^{*}$ | 1.023 | . 002 |
|  |  | 3 months | 3 days | $3.292^{*}$ | 1.023 | . 002 |
|  | snapper | 3 days | 3 months | -. 257 | 1.109 | . 817 |
|  |  | 3 months | 3 days | . 257 | 1.109 | . 817 |
| ground meat | painted | 3 days | 3 months | -11.125* | . 947 | . 000 |
|  |  | 3 months | 3 days | $11.125^{*}$ | . 947 | . 000 |
|  | snapper | 3 days | 3 months | . 714 | 1.013 | . 483 |
|  |  | 3 months | 3 days | -. 714 | 1.013 | . 483 |
| lettuce | painted | 3 days | 3 months | $-12.000^{*}$ | . 947 | . 000 |
|  |  | 3 months | 3 days | $12.000^{*}$ | . 947 | . 000 |
|  | snapper | 3 days | 3 months | -10.381 ${ }^{\text {² }}$ | 1.054 | . 000 |
|  |  | 3 months | 3 days | $10.381^{*}$ | 1.054 | . 000 |

Based on estimated marginal means
*. The mean difference is significant at the .050 level.
b. Adjustment for multiple comparisons: Least Significant Difference (equivalent to no adjustments)

## Main Effects

Using the Food Offered main effect as an example, here is how to get the plot \& follow-ups for that main effect and the corresponding simple effects of Food Offered for each combination of Age \& Species.

## Get the main effect and corresponding simple effect plots

| /PLOT=PROFILE( foodoff ) | $\leftarrow$ gets plot of estimated marginal means |
| :--- | :--- |
| /PLOT=PROFILE( foodoff * age * species ) | $\leftarrow$ gets plot of the cell means arranged to check if the pattern of the |
|  | Food Offered main effect is the same for every combination of Age |
|  | $\&$ Species ( $x$-axis * separate lines * separate graphs) |



None of the simple effects of Food Offered look much like the pattern of the marginal means.



Get estimated marginal means \& follow-up analyses to describe the main effect
/EMMEANS=TABLES ( foodoff) compare ( foodoff)
$\leftarrow$ get pairwise comparisons among marginal means

## Why are the "Descriptive" and "Estimated" marginal means different?

You should notice the estimated marginal means shown in the graphs above and the "Estimates" table below are not the same as the raw marginal means from the "Descriptive Statistics" up above. Those raw marginal means were 12.62 for live crickets, 10.67 for ground meat, and 8.90 for lettuce.

The difference between the raw and estimated marginal means reflects that the effects in the design are not orthogonal (because of unequal-n). The estimated marginal means are predicted based on the model (not the raw data) and provide for the comparisons among these groups, after correcting for the other effects in the model.

## Estimates

Dependent Variable: feeds

| type of food offered | Mean | Std. Error |
| :--- | ---: | ---: |
| live crickets | 12.625 | .377 |
| ground meat | 10.951 | .347 |
| lettuce | 8.887 | .354 |

Univariate Tests
Dependent Variable: feeds

|  | Sum of <br> Squares | df | Mean Square | F | Sig. |
| :--- | :---: | ---: | ---: | ---: | ---: |
| Contrast | 189.142 | 2 | 94.571 | 26.353 | .000 |
| Error | 261.974 | 73 | 3.589 |  |  |

The F tests the effect of type of food offered. This test is based on the linearly
independent pairwise comparisons among the estimated marginal means.

The pattern of the main effect is ...
crickets $v$. meat crickets $v$. lettuce mean v. lettuce
$\ggg>$

The F-test is the same as the test of the Foodoff main effects in the overall analysis up above.

Dependent Variable: feeds

| (l) type of food offered | (J) type of food offered | Mean Difference (I- J) | Std. Error | Sig. ${ }^{\text {b }}$ |
| :---: | :---: | :---: | :---: | :---: |
| live crickets | ground meat | $1.674^{\text { }}$ | . 512 | . 002 |
|  | lettuce | $3.738^{*}$ | . 518 | . 000 |
| ground meat | live crickets | $-1.674^{*}$ | . 512 | . 002 |
|  | lettuce | $2.064^{*}$ | 496 | . 000 |
| lettuce | live crickets | $-3.738^{*}$ | . 518 | . 000 |
|  | ground meat | $-2.064^{*}$ | 496 | . 000 |

Based on estimated marginal means
*. The mean difference is significant at the .050 level.
b. Adjustment for multiple comparisons: Least Significant Difference (equivalent to no adjustments).

Use the related depiction of the 3-way to check the main effects for descriptive/misleading patterns
/EMMEANS=TABLES ( species * age * foodoff ) compare ( foodoff )
$\leftarrow$ gets pairwise comparisons of foodoff cell means at each combination of species age, to check whether the pattern of the foodoff main effect is descriptive or misleading

| Estimates |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Dependent Variable: feeds |  |  |  |  |  |  |  |
| species of turtle | age when turtle was tested |  | type of food offered |  | Mean | Std. Error |  |
| painted | 3 day |  | live crickets |  | 9.333 | . 773 |  |
|  |  |  | ground |  | 1.125 | . 670 |  |
|  |  |  | lettuce |  | 1.250 | . 670 |  |
|  | 3 mon |  | live crick |  | 12.625 | . 670 |  |
|  |  |  | ground |  | 12.250 | . 670 |  |
|  |  |  | lettuce |  | 13.250 | . 670 |  |
| snapper | 3 days |  | live crickets ground meat lettuce |  | 14.143 | . 716 |  |
|  |  |  |  |  | 15.571 | . 716 |  |
|  |  |  |  |  | 5.333 | . 773 |  |
|  | 3 mon |  | live crickets ground meat lettuce |  | 14.400 | . 847 |  |
|  |  |  |  |  | 14.857 | . 716 |  |
|  |  |  |  |  | 15.714 | . 716 |  |
| Univariate Tests |  |  |  |  |  |  |  |
| Dependent Variable: feeds |  |  |  |  |  |  |  |
|  | age when | le was teste | Sum of Squares | df | Mean Square | F | Sig. |
| species of turtle | 3 days | Contrast | 289.610 | 2 | 144.805 | 40.350 | . 000 |
| painted |  | Error | 261.974 | 73 | 3.589 |  |  |
|  | 3 months | Contrast | 4.083 | 2 | 2.042 | . 569 | . 569 |
|  |  | Error | 261.974 | 73 | 3.589 |  |  |
| snapper | 3 days | Contrast | 388.095 | 2 | 194.048 | 54.072 | . 000 |
|  |  | Error | 261.974 | 73 | 3.589 |  |  |
|  | 3 months | Contrast | 5.462 | 2 | 2.731 | . 761 | . 471 |
|  |  | Error | 261.974 | 73 | 3.589 |  |  |

The pattern of the main effect is ...

```
crick v. meat crick v. lettuce mean v. lettuce
```

For 3-day painted, the corresponding simple effect is...

$$
\begin{array}{ccc}
\text { crick v. meat } & \text { crick v. lettuce } & \text { mean v. lettuce } \\
\gg & \gg & =
\end{array}
$$

For 3-month painted, corresponding simple effect is...

| crick v. meat | crick v. lettuce | meanv. lettuce <br> $=$ |
| :---: | :---: | :---: |
| $=$ | $=$ |  |

For 3-day snapper, the corresponding simple effect is...
crick v. meat crick v. lettuce mean v. lettuce

For 3-month snapper, corresponding simple effect is...
crick v. meat crick v. lettuce mean v. lettuce

Pairwise Comparisons

| species of turtle | age when turtle was tested | (l) type of food offered | (J) type of food offered | Mean Difference (l- $\mathrm{J})$ | Std. Error | Sig. ${ }^{\text {b }}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| painted | 3 days | live crickets | ground meat | $8.208{ }^{*}$ | 1.023 | . 000 |
|  |  |  | lettuce | $8.083^{*}$ | 1.023 | . 000 |
|  |  | ground meat | live crickets | -8.208* | 1.023 | . 000 |
|  |  |  | lettuce | -. 125 | . 947 | . 895 |
|  |  | lettuce | live crickets | -8.083 ${ }^{\text {² }}$ | 1.023 | . 000 |
|  |  |  | ground meat | . 125 | . 947 | . 895 |
|  | 3 months | live crickets | ground meat | . 375 | . 947 | 693 |
|  |  |  | lettuce | -. 625 | . 947 | . 511 |
|  |  | ground meat | live crickets | -. 375 | . 947 | . 693 |
|  |  |  | lettuce | -1.000 | . 947 | 295 |
|  |  | lettuce | live crickets | . 625 | . 947 | . 511 |
|  |  |  | ground meat | 1.000 | . 947 | 295 |
| snapper | 3 days | live crickets | ground meat | -1.429 | 1.013 | . 163 |
|  |  |  | lettuce | $8.810^{*}$ | 1.054 | . 000 |
|  |  | ground meat | live crickets | 1.429 | 1.013 | . 163 |
|  |  |  | lettuce | $10.238{ }^{*}$ | 1.054 | . 000 |
|  |  | lettuce | live crickets | $-8.810^{*}$ | 1.054 | . 000 |
|  |  |  | ground meat | -10.238* | 1.054 | . 000 |
|  | 3 months | live crickets | ground meat | -. 457 | 1.109 | .681 |
|  |  |  | lettuce | -1.314 | 1.109 | . 240 |
|  |  | ground meat | live crickets | . 457 | 1.109 | . 681 |
|  |  |  | lettuce | -. 857 | 1.013 | . 400 |
|  |  | lettuce | live crickets | 1.314 | 1.109 | 240 |
|  |  |  | ground meat | . 857 | 1.013 | 400 |

Based on estimated marginal means
*. The mean difference is significant at the .050 level
b. Adjustment for multiple comparisons: Least Significant Difference (equivalent to no adjustments)

So, the main effect marginal mean pattern of Food Offered is not descriptive for any combination of age and species.

