Factorial Designs: Programmatic Research, RH: Testing & Causal Inference

- Applications of Factorial designs in Programmatic Research
- · Research Hypotheses for Factorial Designs
- Variable Role Explication in Factorial Designs & Causal Interpretation

## Using Factorial Designs in Programmatic Research I

Adding a 2<sup>nd</sup> IV

Perhaps the most common application of factorial designs it so look at the separate (main) and combined (interaction) effects of two IVs

Often our research starts with a simple RH: that requires only a simple 2-group BG research design.

Tx1	Control

Keep in mind that to run this study, we made sure that none of the participants had any other treatments !

Factorial Designs – Separate (Main) and combined (interaction) effects of two treatments

At some point we are likely use Factorial designs to ask ourselves about how a  $2^{nd}$  Tx/IV also relates to the DV



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## Using Factorial Designs in Programmatic Research II

## "Correcting" Bivariate Studies

Our well sampled, randomly assigned, manipulated, controlled, carefully measured, properly analyzed study showed ...

Style1 Style2 40 40

... nothing !

Our well sampled, randomly assigned, manipulated, controlled, carefully measured, properly analyzed study showed ...

Context1 Context2 40 40

... nothing !

Looks like neither Style nor Context is related to the DV !!!

Using Factorial Designs in Programmatic Research III Generalization across Populations, Settings & Tasks

Often our research starts with a simple RH: that requires only a simple 2-group BG research design.

Computer Lecture

Keep in mind that to run this study, we had to make some choices/selections:

For example: population  $\rightarrow$  College Students setting  $\rightarrow$  Lecture setting stim/task  $\rightarrow$  teach Psychology

Factorial Design ... Context2 40 20 60 40 40 There are Style effects both for Context1 and Context2 – the marginal Style means are an "aggregation error" There are Context effects both for those in Style1 & Style2 – the marginal Context means are an "aggregation error"

However, when we analyzed

the same data including both

variables as IVs in a

So, instead of the "neither variable matters" bivariate results, the multivariate result shows that both variables are conditionally related to the DV -- they interact !!!!! BOTH are important!!! ō



When we've found and replicated an effect, making certain selections, it is important to check whether changing those selections changes the results – by running factorials with the external validity elements as  $2^{nd}$  lvs and looking for interactions!



If there are no interactions – if the results "don't depend upon" the population, task/stimulus, setting, etc – we need to know that, so we can apply the results of the study to our theory or practice, confident in their generalizability

If there are an interactions – if the results "depend upon" the population, task/stimulus, setting, etc – we need to know that, so we can apply the "correct version" of the study to our theory or practice



• other populations – college vs. high school

• other settings - lecture vs. laboratory

other tasks/stimuli – psyc vs. philosophy



 Tx
 Control
 Tx
 Control

 Psyc
 Image: Control
 Lecture
 Image: Control

 Phil
 Image: Control
 On-line
 Image: Control



## Using Factorial Designs in Programmatic Research IV

Do effects "depend upon" length of treatment ?

As before, often our research starts with a simple RH: that requires only a simple 2-group BG research design.



**Time Course Investigations** 

In order to run this study we had to select ONE treatment duration (say 16 weeks):

- we assign participants to each condition
- begin treatment of the Tx groups
- treat for 16 weeks and then measured the DV

Using this simple BG design we can "not notice" some important things. A MG Factorial can help explore the time course of the Tx effects.

By using a MG design, with different lengths of Tx as the 2<sup>nd</sup> IV, we might find different patterns of data that we would give very different interpretations



Short Medium Tx<sub>1</sub> 20 40

40

20

 $Tx_2$ 

	Short	Medium		Short	Medium		Short	Medium
Tx <sub>1</sub>	20	40	Tx <sub>1</sub>	20	40	Tx <sub>1</sub>	20	0
Tx <sub>2</sub>	20	20	Tx <sub>2</sub>	20	60	Tx <sub>2</sub>	20	40

## Using Factorial Designs in Programmatic Research V

Evaluating Initial Equivalence when Random assignment is not possible

As before, often our research starts with a simple RH: that requires only a simple 2-group BG research design.



Initial Equivalence Investigations

In order to causally interpret the results of this study, we'd have to have initial equivalence

- but we can't always RA & manipulate the IV
- So what can we do to help interpret the post-treatment differences of the two treatments?
- Answer compare the groups before treatment too!



## Replication & Generalization in Easterial Designs, cont...

Most factorial designs are an "expansion" or an extension of an earlier, simpler design, often by adding a second IV that "makes a variable out of an earlier constant". This second IV may related to the population, setting or task/stimulus involved.

Study #1 – Mix of Networked &
Stand-alone computers

### Study #2



What gives us the most direct replication? The main effect of PC vs. Mac or one of the SEs of PC vs. Mac?

#### PC Mac 8.9 1.6 Networked Stand-alone 3.1 5.8 6.0 3.7

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#### Did Study #2 replicate Study #1?

## Replication & Generalization in Factorial Designs

Most factorial designs are an "expansion" or an extension of an earlier, simpler design, often by adding a second IV that "makes a variable out of an earlier constant". This second IV may related to the population, setting or task/stimulus involved.

Study #1 – Graphical software

Study #2

Mean failures $PG = 5.7$ , sto = 2.1	
Mean failures Mac = 3.6, std = 2.	. 1

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	PC	Mac	
Graphical	5.9	3.6	
Computing	3.1	3.8	
	4.5	3.7	

Did Study #2 replicate Study #1?

# **RH: for Factorial Designs**

Research hypotheses for factorial designs may include

- RH: for main effects
  - involve the effects of one IV, while ignoring the other IV
  - tested by comparing the appropriate marginal means
- RH: for interactions
  - usually expressed as differences between hypothesized results for a set of simple effects
  - tested by comparing the results of the appropriate set of simple effects
  - That's the hard part -- determining which set of simple effects gives the most direct test of the interaction RH:

- #1 Sometimes the Interaction RH: is explicitly stated
  - when that happens, one set of SEs will provide a direct test of the RH: (the other won't) Presentation

Here's an example:

Easy tasks will be performed equally well using paper or computer presentation, however, hard tasks will be performed better using computer presentation than paper.



This is most directly tested by inspecting the simple effect of paper vs. computer presentation for easy tasks, and comparing it to the simple effect of paper vs. computer for hard tasks.



#2 Sometimes the set of SEs to use is "inferred" ...

Often one of the IVs in the study was used in previous research, and the other is "new".

- In this case, we will usually examine the simple effect of the "old" variable, at each level of the "new" variable
- •this approach gives us a clear picture of the replication and generalization of the "old" IV's effect.

e.g., Previously I demonstrated that computer presentations lead to better learning of statistical designs than does using a conventional lecture. I would like to know if the same is true for teaching writing.

Let's take this "apart" to determine which set of SEs to use to examine the pattern of the interaction...

SE Topic @ Major

Previously I demonstrated that computer presentations lead to better learning of statistical designs than does using a conventional lecture. I would like to know if the same is true for teaching writing.



Your turn ..

I have previously demonstrated that rats learn Y-mazes faster than do hamsters. I wonder if the same is true for radial mazes ?



I've discovered that Psyc majors learn statistics & Ethics about equally well. My next research project will also look at how well Sociology majors learn these topics.





#3 Sometimes the RH: about the interaction and one about the main effects are "combined"

 this is particularly likely when the expected interaction pattern is of the > vs. > type (the most common pattern)



Your Turn...

Young children have better verbal skills than motor skills, however the difference gets smaller with age (DV = skill score) e Type of Skill Motor 4 yrs 9 yrs SE Skill @ Age



Confession is considered more convincing than eyewitness testimony. This preference is stronger for jurors than judges.

(DV = convincingness rating)

Age

SE Evidence @ Rater

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