# **Comparing a Multiple Regression Model Across Criterion Variables**

Sometimes we have multiple behaviors or responses that might be used as criterion variables. When this happens we might want to determine whether the models to predict the different criterion differ. This can be a useful way of determining whether or not behaviors or responses represent "the same thing".

For example we might have two different criteria by which we assess the "performance" of 1<sup>st</sup> year graduate students: 1) their grades and 2) the number of presentations and/or publications they obtain or collaborate on during their first year. Are the multiple regression models for predicting these two from GRE scores "the same"?

First we get the multiple regression model for each criterion, in turn. Here's the abbreviated output ...

## For GPA as the criterion

## For #pubs & presentations as the criterion

Model Summary

Model	Summary
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Model	R	R Square	Adjusted R Square	Std. Error of the Estimate
1	.756 <sup>a</sup>	.572	.563	.39752

 Predictors: (Constant), Verbal subscore of GRE, Quantitative subscore of GRE, Analytic subscore of GRE

### Coefficients<sup>a</sup>

		Unstand ardized Coefficie nts	Standa rdized Coeffic ients	
Model		В	Beta	Sig.
1	(Constant)	-1.215		.003
	Analytic subscore of GRE	6.78E-03	.551	.000
	Quantitative subscore of GRE	3.42E-03	.462	.000
	Verbal subscore of GRE	-2.3E-03	235	.001

a. Dependent Variable: 1st year graduate gpa -- criterion variable

Model	R	R Square	Adjusted R Square	Std. Error of the Estimate
1	.917 <sup>a</sup>	.842	.838	.24176

 Predictors: (Constant), Verbal subscore of GRE, Quantitative subscore of GRE, Analytic subscore of GRE

Coefficients<sup>a</sup>

		Unstan dardize d Coeffici ents	Stand ardize d Coeffi cients	
Model		В	Beta	Sig.
1	(Constant)	7.706		.000
	Analytic subscore of GRE	1.1E-04	.009	.827
	Quantitative subscore of GRE	4.0E-04	.058	.152
	Verbal subscore of GRE	8.6E-03	.893	.000

a. Dependent Variable: PUBPRES

Inspection of the  $\boldsymbol{\beta}$  weights of the two models suggests that:

- The fit of the two models to the criteria appears to be different -- R<sup>2</sup> = .572 for GPA and .842 for publications/presentations.
- There is no direct test of these correlations -- can't use Fisher's Z-test because the models are from the same sample & can't use Hotelling's/Meng, etc. tests because both the criterion and the predictors producing the R values are different.
- The models appear to have very different "structures"
- Prediction of 1<sup>st</sup> year GPA involves all three GRE subscales (with somewhat less contribution from the suppressor variable GREV)
- Prediction of 1<sup>st</sup> year #publications/presentations involves only GREV, in this sample.
- To formally compare these models we will need to ...
- Apply both models to the prediction of a single criterion (we'll use GPA)
- Compare the R obtained from these applications, taking the correlation between the models into account

We'll need to compute a predicted GPA score based on each model, in turn ...



Finally, we get the correlation of each model with the selected criterion variable, as well as the correlation between the models.

🔀 Bivariate Correlations	:	×
<ul> <li>♣ subn</li> <li>♠ program</li> <li>♣ grea</li> <li>♣ greq</li> <li>♣ grev</li> <li>♣ pubpres</li> <li>♣ pubpres2</li> </ul>	Variables:	OK <u>P</u> aste <u>R</u> eset Cancel Help
Correlation Coefficients		
Pearson 🗖 Kenda	all's tau-b 🔲 <u>S</u> pearman	
- Test of Significance		
	🔿 One-tailed	
Elag significant correlati	ons	Options

### **SPSS Syntax**

COMPUTE gpadir = (.00678\*grea) + (.00342\*greq) + (-.0023\*grev) - 1.215. COMPUTE gpacros = (.00011\*grea) + (.0004\*greq) + (.0086\*grev) - 7.706.

CORR VARIABLES = gpa gpa\_dir gpa\_cros.

- ← compute the direct model y'
- compute the crossed model y'
- ← compute the correlations

Here's the output...



## Remember that the "Hotellings t/ Steiger's Z" part of the FZT program uses R (r) values!

Applying the FZT program with  $r_{y1}$  = .756,  $r_{y2}$  = .310 and  $r_{12}$  = .406 and N = 140 gives t = 7.32 & Z = 6.33

So, the apparent differences between the structures of the multiple regression models for predicting these two criterion variables were revealed by the formal statistical comparison. The substantive implication of this finding is that the graduate faculty need to decide which criterion they want to predict, because the model for the two criterion isn't "interchangeable" -- that is predicting 1<sup>st</sup> year GPA is not the same as predicting 1<sup>st</sup> year #pubs/presentations (by the way, these two criterion variables are correlated -.285 in this sample).

#### Example write-up of these analyses (which used some univariate and correlation analyses not shown above):

Separate regression analyses were run using the Verbal (GREV), Quantitative (GREQ) and Analytic (GREA) GRE subscales to predict the two criterion variables graduate grade point average (GGPA) and the number of graduate publications and presentations (NGPP). Table 1 shows the univariate statistics and Table 2 shows the correlations of each variable with respective criterion variables and the multiple regression weights for the models of the two criterion variables.

The graduate grade point average model had an  $R^2 = .572$ , F(3,138) = 35.65, p < .001, with all three GRE scores having significant regression weights and GREA and GREQ seeming to have the major contributions (based on inspection of the  $\beta$  weights). The number of publications and presentations model had an  $R^2 = .842$ , F(3,138) = 72.53, p < .001, with only GREV having significant a regression weight.

A comparison of the structure of the models for the two criterion variables was also conducted by applying the model derived from number of publications and presentations criterion to graduate grade point average and comparing the resulting "crossed" R<sup>2</sup> with the "direct" R<sup>2</sup> originally obtained for this criterion. The direct R<sup>2</sup>=.572 and crossed R<sup>2</sup>=..096 were significantly different, Z = 6.33, p < .01, which indicates that the apparent differential structure of the regression weights derived for the two criteria described above warrants further interpretation and investigation.

Table 1 Summary statistics for criterion and predictor variables.

Variable	mean	std
NGPP	11.21	3.32
GGPA	3.23	.61
GREV	567.88	40.99
GREQ	589.62	82.01
GREA	576.03	66.86

Table 2 Correlations and multiple regression weights from models of graduate grade point average and number of publications and presentations.

Graduate Grade Point Average		Number of Publications & Presentations				
Variable		h	o		h	o
variable	GGPA	D	р	NPP	D	р
GREV	.270	0023**	235	.839**	.0086**	.893
GREQ	.479**	.0034**	.462	.320*	.0044	.058
GREA	.632**	.0068**	.551	.194	.0011	.009
constant		-1.215			7.706	

\* p < .05 \*\* p < .01